#### **Fatigue and Fracture**

Factors Influencing Fatigue Mean Stress

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# **Factors Influencing Fatigue**

#### Mean Stress

Variable Amplitude

- Stress Concentrations
- Surface Finish





- Tensile mean stresses reduce the fatigue life or decrease the allowable stress range
- Compressive mean stresses increase the fatigue life or increase the allowable stress range







Fatigue damage is a shear process

Tensile mean stresses open microcracks and make sliding easier





*Mechanics Applied to Engineering* John Goodman, 1890

".. whether the assumptions of the theory are justifiable or not .... We adopt it simply because it is the easiest to use, and for all practical purposes, represents Wöhlers data.

$$S_{\text{ultimate}} = S_{\text{min}} + 2 \Delta S$$



FIG. 517.







# Modified Goodman (no yielding)



### Mean Stress Influence on Life



### **Stress Concentrations**



The elastic material surrounding the plastic zone around a stress concentration forces the material to deform in strain control



Nominal mean stress is less than notch mean stress

Nominal mean stress is greater than notch mean stress

#### **Morrow Mean Stress Correction**



### **Smith Watson Topper**



### **Mean Stress Relaxation**



FIG. 7—Cyclic softening and relaxation of mean stress under Neuber control (Ti-8Al-1Mo-IV,  $K_t = 1.75$ ).

Stadnick and Morrow, "Techniques for Smooth Specimen Simulation of Fatigue Behavior of Notched Members" ASTM STP 515, 1972, 229-252

# Loading Histories







Load History B

### **Test Results**







ASTM STP 1389,2000, 3-38

Factors Influencing Fatigue





#### Crack open



#### Crack closed



Compressive stresses are not very damaging in crack growth

### Sources of Mean/Residual Stress

- Loading History
- Fabrication
- Shot Peening
- Heat Treating



Tension overloads produce favorable compressive residual stress

#### Compressive overloads produce unfavorable tensile residual stress



#### **Fabrication**



### **Cold Expansion**

#### 1965 Basic Cx process conceptualized (Boeing)



Courtesy of Fatigue Technology Inc.

# **Theory of Cold Expansion**



Courtesy of Fatigue Technology Inc.

### Fatigue Life Improvement



Courtesy of Fatigue Technology Inc.





Residual stress in a shot peened leaf spring

### **Shot Peening Results**



www.metalimprovement.com





50 mm diameter induction hardened 1045 steel shaft

# Things Worth Remembering

- Local mean stress rather than the nominal mean stress governs the fatigue life
- Mean stress has the greatest effect on crack nucleation

# **Factors Influencing Fatigue**

- Mean Stress
- Variable Amplitude
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#### How to you identify cycles ?

How do you assess fatigue damage for a cycle ?

# **Rainflow Cycle Counting**





图6. 重量激尖顶值+系列值、



# What could be more basic than learning to count correctly?

Matsuishi and Endo (1968) Fatigue of Metals Subjected to Varying Stress – Fatigue Lives Under Random Loading, Proceedings of the Kyushu District Meeting, JSME, 37-40


#### **Rainflow and Hysteresis**



**Factors Influencing Fatigue** 

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Miner's Rule:

$$Damage = \sum \frac{n}{N_F} = \frac{n_H}{N_{f H}} + \frac{n_L}{N_{f L}}$$



#### **Periodic Overload Results**



Bonnen and Topper, "The Effects of Periodic Overloads on Biaxial Fatigue of Normalized SAE 1045 Steel" ASTM STP 1387, 2000, 213-231

**Factors Influencing Fatigue** 

## **Fatigue Damage Calculations**



Damage  $\propto \Delta S^{10}$ 

#### **Crack Growth Data**







Which cycles do the most fatigue damage?

(a) a few large cycles

(b) a moderate number of intermediate cycles

(c) a large number of small cycles



# Loading History









# Mechanisms and Slopes





Equivalent constant amplitude loading

$$\Delta \overline{S} = \sqrt[n]{\frac{\sum_{i=1}^{N} \Delta S_i^{n}}{N}}$$

Typically n ranges from 4 to 6 for structures

N cycles at an amplitude of  $\Delta \overline{S}$  does as much damage as the entire loading history

# SAE Keyhole Specimen





### SAE Keyhole Test Data



# **Things Worth Remembering**

- Rainflow counting is employed to identify cycles
- The slope of the fatigue curve (damage mechanism) has a large influence on how much damage is caused by smaller cycles

# **Factors Influencing Fatigue**

- Mean Stress
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## **Stress Concentration Factor**











Stress calculated with elastic assumptions

#### Neuber's Rule for Fatigue

Stress and strain amplitudes

	$K_t \Delta S K_t \Delta e$		_ ΔσΔε
	2	2	2 2
Elastic nominal stress			
	$\Delta$	$\Delta e = \Delta s$	5
		2 2E	
Substitute and rearrang	е		

$$K_t \frac{\Delta S}{2} = \sqrt{E \frac{\Delta \sigma}{2} \frac{\Delta \varepsilon}{2}}$$

The product of stress times strain controls fatigue life



Stress analysis and stress concentration factors are independent of size and are related only to the ratio of the geometric dimensions to the loads

Fatigue is a size dependent phenomenon

How do you put the two together ?





#### Fatigue of Notches



From Dowling, Mechanical Behavior of Materials, 1999





Large Notch

**Small Notch** 





#### Low Strength

**High Strength** 



Low K<sub>t</sub>

High K<sub>t</sub>

















Stress concentrations are not very important at short lives
#### Fatigue of Notches



From Dowling, Mechanical Behavior of Materials, 1999

#### **Crack Growth Data**



Nonpropagating cracks

$$\Delta K_{TH} > \Delta \sigma 1.12 \frac{2}{\pi} \sqrt{\pi a}$$





Frost, "A Relation Between the Critical Alternating Propagation Stress and Crack Length for Mild Steel" Proceedings of the Institute for Mechanical Engineers, Vol. 173, No. 35, 1959, 811-836

Factors Influencing Fatigue

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For  $K_t > 4$ , the notch acts like a crack with a depth D

$$S_{fl} = \frac{\Delta K_{th}}{\sqrt{\pi D}}$$

K<sub>t</sub> does not play a role for sharp notches !

A stress concentration behaves like a crack once a stress concentration becomes large (Kt > 4)









Once a crack reaches 10% of the hole radius, it behaves as if the hole was part of the crack

#### **Specimens with Similar Geometry**



#### Ultimate Strength 780 MPa Yield Strength 660 MPa





## **Things Worth Remembering**

- Fatigue may be thought of as a failure of the average stress concept, consequently, fatigue usually begins at stress concentrators which are most frequently located on the surface
- The severity of a stress concentrator in fatigue is size dependent
- Small stress concentrators are more effective in high strength materials

## **Factors Influencing Fatigue**

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#### Modern View of the Fatigue Limit

The fatigue limit is the stress where a crack may nucleate but will not grow through the first microstructural barrier such as the grain size, pearlite colony size, prior austenite grain size, eutectic cell size or precipitate spacing.





**Slip Bands** 

Crack







Little effect of surface pit because it is smaller than the grain size Large effect of defect because it is larger than the grain size

#### Surface Finish Influence

<u>Method</u> Stress-Life Strain-Life Crack Growth Physics Crack Nucleation Microcrack Growth Macrocrack Growth <u>Size</u> 0.01 mm 0.1 - 1 mm > 1mm Influence of Surface Finish Strong Moderate None

## Sources of Surface Effects

- Machining
  - Cutting
  - Grinding
- Corrosion
  - General
  - Pitting
- Processing
  - Cutting/Shearing
  - Casting
  - Forging
  - Plating
- Foreign Object Damage
  - Nicks
  - Scratches







# Cracks start in machining marks not in the direction of the maximum principal stress

# Casting



 $100 \ \mu m$ 

#### Surface flaw in gray cast iron

#### **Nodular Iron Surface**



#### Flake graphite formed on the surface of a nodular iron casting

Starkey and Irving, "A Comparison of the Fatigue Strength of Machined and As-cast Surfaces of SG Iron" International Journal of Fatigue, July, 1982, 129-136

**Factors Influencing Fatigue** 

#### Test Data



#### **Surface Reduction Factors**



#### Noll and Lipson 1945



#### Hiam and Pietrowski 1978



Driven for 1 or 2 years in Southern Ontario before making specimens to evaluate corrosion effects

Strain controlled fatigue testing

Hiam and Pietrowski, "The Influence of Forming and Corrosion on the Fatigue Behavior of Automotive Steels", SAE Paper 780040, 1978



	Hot Rolled Surface	Corroded Surface
950X	1.12	1.49
0.06% C HSLA	1.18	1.65
0.18% C HSLA		1.90

Surface finish factor predicts  $K_f = 1.6$  for a Hot Rolled Surface

from Hiam and Pietrowski

**Factors Influencing Fatigue** 

#### Pit Depth Effects on Life



## **Fatigue Notch Factor for Pits**







## **Spring Failures**







#### **Corrosion Pits**

#### **Chrome Plating**



Almen, "Fatigue Loss and Gain by Electroplating", Product Engineering, Vol. 22, No. 5, 1951, 109-116

#### Hard Chrome Plating



In addition to cracks, coatings frequently have high tensile residual stresses

Metals Handbook, Volume 9, Fractography and Atlas of Fractographs



Vogt, Boussac, Foct, "Prediction of Fatigue Resistance of a Hot-dip Galvanized Steel" Fatigue and Fracture of Engineering Materials and Structures, Vol. 23, No. 1, 2001,33-40

## Fatigue Limit for Galvanized Steel



Coatings can be modeled with a crack equal to the coating thickness

#### **Anodized Aluminum**



Rateick et. al. "Relationshipp of Microstructure to Fatigue Strength Loss in Anodized Aluminum-Copper Alloys" Aeromet 2004, June 2004

**Factors Influencing Fatigue** 

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# Pitting at Cu Rich Constituent



- AA2219-T851 plate cross sectioned immediately after anodizing
- A: Pits
- B: Cu rich constituent

#### Foreign Object Damage



http://www.eng.ox.ac.uk/~ftgwww/frontpage/fod2.html

#### Foreign Object Damage



http://www.eng.ox.ac.uk/~ftgwww/frontpage/fod2.html
## Upper Control Arm



## Serial Number



## **Things Worth Remembering**

- Fatigue crack nucleation is a surface phenomena and everything about the surface affects the fatigue life
- Most of the design rules are conservative having been developed for materials of the 1950's

## **Fatigue and Fracture**

